

BACKGROUND KNOWLEDGE FOR CALCULUS

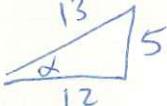
1. Area of a square with side s : $A = s^2$
2. Area of a rectangle with width w and length l : $A = l w$
3. Area of a right triangle with base b and height h : $A = \frac{bh}{2}$
4. Area of a circle with radius r : $A = \pi r^2$
5. Circumference of a circle with radius r : $C = 2\pi r$
6. Volume of a box with width w , length l and height h : $V = lwh$
7. Volume of a cylinder (i.e., a can) with radius r and height h : $V = \pi r^2 h$
8. Surface area of a cylinder with radius r and height h : $2\pi r h + 2\pi r^2$
9. Pythagorean Theorem: $h = \sqrt{a^2 + b^2}$
10. Diagonal of a square with side s : $d = s\sqrt{2}$
11. Side of a square with diagonal d : $s = \frac{d}{\sqrt{2}}$
12. Quadratic formula (to find roots of $ax^2 + bx + c = 0$): $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
13. Expansion of $(a + b)^2$: $a^2 + 2ab + b^2$
14. Expansion of $(a - b)^2$: $a^2 - 2ab + b^2$
15. Definition of $\sin \alpha$ in terms of sides of a triangle: opp/hyp
16. Definition of $\cos \alpha$ in terms of sides of a triangle: adj/hyp
17. Definition of $\tan \alpha$ in terms of sides of a triangle: opp/adj
18. The values of $\sin \alpha$, $\cos \alpha$, $\tan \alpha$, if α is $30^\circ = \pi/6$: $\frac{1}{2}, \frac{\sqrt{3}}{2}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}$
19. The values of $\sin \alpha$, $\cos \alpha$, $\tan \alpha$, if α is $60^\circ = \pi/3$: $\frac{\sqrt{3}}{2}, \frac{1}{2}, \frac{1}{\sqrt{3}}$
20. The values of $\sin \alpha$, $\cos \alpha$, $\tan \alpha$, if α is $45^\circ = \pi/4$: $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 1$
21. The values of $\sin \alpha$, $\cos \alpha$, $\tan \alpha$, if α is 0° : $0, 1, 0$
22. The values of $\sin \alpha$, $\cos \alpha$, $\tan \alpha$, if α is $90^\circ = \pi/2$: $1, 0, \infty$
23. The values of $\sin \alpha$, $\cos \alpha$, $\tan \alpha$, if α is $180^\circ = \pi$: $0, -1, 0$
24. True or False?: $\sqrt{a^2 + b^2} = a + b$. Why (not) (i.e., prove or give a counter-example)?

False NO $\sqrt{1+1} = \sqrt{2}$ $\sqrt{1+1} = 1+1=2$

25. What is $\sin 2x$ in terms of trig functions of x ? $\sin 2x = 2 \sin x \cos x$

26. What is $\sin^2 x$ in terms of trig functions of $2x$? $\sin^2 x = \frac{1 - \cos 2x}{2}$

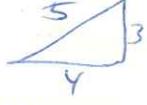
27. What is $\cos^2 x$ in terms of trig functions of $2x$? $\cot^2 x = \frac{1 + \cos 2x}{2}$
28. What is the standard trig version of the pythagorean theorem (i.e., inter-relate $\sin x$ and $\cos x$ somehow)? $\sin^2 x + \cos^2 x = 1$
29. Given $\sin \alpha = 5/13$. what is $\cot \alpha$? $12/5$
30. Given $\sin \alpha = 4/5$, what is $\sin 2\alpha$? $24/25$
31. Calculate the area of a circle, given that the circumference equals 10π . 25π
32. Calculate the area of a right triangle, with one side equaling 3 and the hypotenuse equaling 5. 6

29. $\sin \alpha = \frac{5}{13}$


30. $\sin \alpha = 4/5$


$$\begin{aligned} \sin 2\alpha &= 2 \sin \alpha \cos \alpha \\ &= 2 \cdot \frac{4}{5} \cdot \frac{3}{5} \\ &= \frac{24}{25} \end{aligned}$$

31. $C = 10\pi = 2\pi r$
 $r = 5$
 $A = \pi r^2 = 25\pi$

32. $A = \frac{bh}{2}$

 $= \frac{3 \cdot 4}{2} = \frac{12}{2} = 6$